Adapting Human Motions to Humanoid Robots Through Time Warping Based on a General Motion Feasibility Index

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Abstract-Having human-like motions will make humanoid robots more predictable and safer for the people around them. An effective way to realize this would be to use human motions as reference. Due to different kinematic and dynamic properties between humans and humanoid robots, however, a human motion could be physically infeasible for a robot and cause the robot to fall over. Therefore, it is necessary to modify and adapt an infeasible human motion to the robot. This paper presents a method for adapting human motions to humanoid robots based on a technique called time warping, which modifies the time line of a reference motion to speed up or slow down the motion. By doing this, the velocity and acceleration profiles of the motion are changed and it is possible to turn an infeasible motion into a feasible one. The optimal time warping is obtained through a generalized motion feasibility index that quantifies the feasibility of a motion considering the friction and center-ofpressure constraints. Thanks to the generality of the index, the proposed motion adaptation method can be applied to motions on arbitrary terrains or number of links in contact with the environment. Through dynamics simulation, we demonstrate that the method facilitates the reproduction of human motions on a humanoid robot.

I. INTRODUCTION

Humanoid robots are built to resemble humans and expected to assist and live with people in the future. Having human-like movements together with human-like appearances helps people infer their future motion and intention, which is of great importance for safe and smooth humanrobot interactions. However, it is difficult to generate humanlike motions through optimization or control because no clear criterion is known for coordinating all the joints such that the resulting motions look human-like. For example, many locomotion controllers for humanoid robots are based on simple models that cannot describe their full-body motion, so the motions usually do not look like a human [8], [7]. In computer graphics, some methods have successfully generated human-like walking and running motions on virtual characters [26], [12], but it is hard to extend them to stylized motions.

Since humanoid robot body is designed to resemble that of humans, mimicking human motions seems a natural and promising way to endow humanoid robots with human-like movements. Due to kinematic/dynamic differences between humans and robots, however, a human motion can be infeasible for a robot and cause the robot to fall over. To solve this issue, human motions are usually adapted to the robot's kinematics and dynamics. A potential issue with this approach is that the modified motion may not satisfy other constraints, such as footstep location in locomotion.

In this paper, we adapt a reference human motion to a humanoid robot by modifying the time line of the motion, called time warping, which implies that the robot will realize the same poses as in the reference motion at different moments. By doing this, the velocity and acceleration profiles of the motion are changed and the reference motion can be turned into a feasible motion for the robot. To ensure that the motion will not be disordered or prolonged by time warping, we choose a strictly increasing function that preserves the period of time of the motion to map the original time line to a new one. A general motion feasibility index is proposed to guide the choice of a time warping function such that the modified motion has a relatively larger feasibility margin for the robot. Thanks to the generality of the index, the proposed motion adaptation method can be applied to motions on arbitrary terrains or contact situations.

The rest of this paper is organized as follows. Section II reviews the related work. Section III goes over the dynamics of a humanoid robot. Section IV discusses the motion feasibility index, followed by the motion adaptation through time warping in Section V. Section VI shows simulation results. Conclusion and future work are given in Section VII.

II. RELATED WORK

As humanoid robots and humans have similar structures, programming humanoid robots by referring to human motions seems to be an effective way to let robots have natural human-like movements. Many efforts have been made to this end. Some methods calculate the joint angles of a robot to fit a human motion based purely on the kinematics of a robot [1], [17]. Some methods parameterize the joint trajectory of a robot and formulate an optimization problem to determine the values of parameters, respecting the fitting to the reference trajectory as well as robot's own dynamics and physical limitations [19], [16], [18]. Many methods modify the joint trajectory extracted from a human motion according to a replanned zero moment point (ZMP) or center of mass (CoM) trajectory, which is generated based on a simple model of the robot and ensures the equilibrium of the robot in the motion [3], [13], [10], [2]. Rather than offline planning, other methods can realize online motion tracking incorporated with balance control [14], [22], [23], [20], [11].

All the aforementioned methods modify the pose of the robot in a motion in order to make the motion feasible for the robot. In fact, the velocity and acceleration profiles of a

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motion can be changed without changing the pose by scaling or warping the time line of the motion. By this means, it is possible to obtain a feasible motion in which the robot will realize the same pose as specified in the original reference motion. This idea was used for modifying the trajectory of manipulators subject to the joint torque limit [6].

In order to adapt human motions to humanoid robots, a criterion for quantifying motion feasibility is needed. The most widely used criterion is the Zero-Moment Point (ZMP) [21] that represents the center of the ground reaction force required to perform a given motion. The motion is feasible if the ZMP is always within the contact convex hull. Kanehiro et al. [9] used the ZMP criterion to determine the time progress to generate collision-free and dynamically feasible motions. Goswami [4] proposed the foot rotation indicator (FRI) that indicates the center of ground reaction force required to keep the foot stationary. However, they do not consider the friction constraint at contact and assume that all contacts occur on a flat surface. More general criteria based on feasible contact forces have been used in walking pattern generation [5], balance control [15], and motion tracking [28] of humanoid robots. In this paper, we present a general motion feasibility index that considers friction constraints and allows complex contact conditions and apply the index to human motion adaptation.

III. MOTION TRACKING CONTROL

To better understand the issue, we first review the dynamics and motion tracking of a humanoid robot in this section.

A. Equation of Motion

We consider a humanoid robot with N_J actuated joints and $N_G = N_J + 6$ degrees of freedom (DoF) including the six unactuated DoF of the floating base. Let $q \in \mathbb{R}^{N_G}$ denote the generalized coordinates that define the configuration of the robot and the first six components of q correspond to the translation and rotation of the floating base of the robot. Let N_C be the number of links in contact with the environment and $w_i \in \mathbb{R}^6$ $(i = 1, 2, ..., N_C)$ the contact wrench (force and moment) applied to contact link i by the environment.

The equation of motion of the robot can be written as

$$M\ddot{q} + c = N^T \tau + J^T w \tag{1}$$

where $\boldsymbol{M} \in \mathbb{R}^{N_G \times N_G}$ is the generalized-coordinatespace inertia matrix of the robot, $\boldsymbol{c} \in \mathbb{R}^{N_G}$ is the sum of Coriolis, centrifugal and gravity forces, and $\boldsymbol{w} = [\boldsymbol{w}_1^T \ \boldsymbol{w}_2^T \ \dots \ \boldsymbol{w}_{N_C}^T]^T \in \mathbb{R}^{6N_C}$. Matrix $\boldsymbol{N} \in \mathbb{R}^{N_J \times N_G}$ maps the joint torques into the generalized forces. Since the floating base is unactuated, the first six rows of \boldsymbol{N}^T are zero and \boldsymbol{N} has the form

$$\boldsymbol{N} = \begin{bmatrix} \boldsymbol{0}_{N_J \times 6} & \boldsymbol{I}_{N_J \times N_J} \end{bmatrix}.$$
(2)

Matrix $J \in \mathbb{R}^{6N_C \times N_G}$ is the contact Jacobian and its transpose maps the contact wrenches into the generalized forces and has the form

$$\boldsymbol{J} = \begin{bmatrix} \boldsymbol{J}_1^T & \boldsymbol{J}_2^T & \dots & \boldsymbol{J}_{N_C}^T \end{bmatrix}^T$$
(3)



Fig. 1. Illustration of the relation between the wrench and the contact forces applied to a contact link by the environment.

where $J_i \in \mathbb{R}^{6 \times N_G}$ is the Jacobian of contact link *i* with respect to the generalized coordinates.

Let $p_{i,j} \in \mathbb{R}^3$ $(j = 1, 2, ..., N_i)$ be the vertices of the contact area between contact link *i* and the environment, and $f_{i,j} \in \mathbb{R}^3$ the contact force at vertex *j* on contact link *i*, as depicted in Fig. 1. The number N_i of contact vertices for every contact link can be 0, 1, 2, and 3 or more in the cases of no contact, point contact, edge contact, and face contact, respectively. We assume that all the contacts are rigid subject to Coulomb friction model. Therefore, $f_{i,j}$ is a pure force and can be decomposed into three components $f_{i,j1}, f_{i,j2}, f_{i,j3}$ along the normal and two tangential vectors at the contact vertex, and it must satisfy the friction constraint as below to avoid undesired slippage at the contact link,

$$F_{i,j} = \left\{ \mathbf{f}_{i,j} \in \mathbb{R}^3 \mid f_{i,j1} \ge 0, \ \sqrt{f_{i,j2}^2 + f_{i,j3}^2} \le \mu_i f_{i,j1} \right\}.$$
(4)

The wrench w_i applied to contact link *i* is the resultant force and moment from all contact forces $f_{i,j}$ $(j = 1, 2, ..., N_i)$ and can be written as

$$\boldsymbol{w}_i = \sum_{j=1}^{N_i} \boldsymbol{R}_{i,j} \boldsymbol{f}_{i,j} = \boldsymbol{R}_i \boldsymbol{f}_i$$
(5)

where $\mathbf{R}_i = [\mathbf{R}_{i,1} \ \mathbf{R}_{i,2} \ \dots \ \mathbf{R}_{i,N_i}] \in \mathbb{R}^{6 \times 3N_i}, \ \mathbf{f}_i = [\mathbf{f}_{i,1}^T \ \mathbf{f}_{i,2}^T \ \dots \ \mathbf{f}_{i,N_i}^T]^T \in \mathbb{R}^{3N_i}, \text{ and } \mathbf{R}_{i,j} \in \mathbb{R}^{6 \times 3}$ is the matrix that maps $\mathbf{f}_{i,j}$ into the force and moment around the local frame of contact link *i* in which w_i is expressed.

B. Inverse Dynamics

In order for a humanoid robot to realize a reference human motion, right joint torques need be determined for actuating the robot. To do this, the desired joint accelerations are first calculated based on the reference accelerations as well as the reference and current positions and velocities of joints:

$$\hat{\ddot{\boldsymbol{q}}} = \ddot{\boldsymbol{q}}^{ref} + k_d (\dot{\boldsymbol{q}}^{ref} - \dot{\boldsymbol{q}}) + k_p (\boldsymbol{q}^{ref} - \boldsymbol{q})$$
(6)

where q, \dot{q} are the current joint angle and velocity, q^{ref} , \dot{q}^{ref} , \ddot{q}^{ref} are the reference joint angle, velocity, and acceleration, and k_p , k_d are proportional and derivative gains, which can be different for different joints.

Once the desired joint accelerations are determined, joint torques and corresponding contact forces are computed based

on (1) and (5) subject to the friction constraint (4). This problem is often known as inverse dynamics and can be reduced to a quadratic programming problem [22], [28], [11]. For more details, readers are referred to relevant references.

It is quite common that a reference motion is not always feasible for the robot. In other words, there may not exist feasible contact forces under the friction constraint to support the robot and enable the robot to realize the desired joint accelerations. In this case, the reference motion will not be exactly reproduced, and what motion the robot will generate depends on the property of the motion tracking controller and the extent of infeasibility of the reference motion. Sometimes a similar motion may be generated, but an unexpected motion may also occur and cause the robot to fall over. Therefore, it is necessary to modify the motion and make it feasible for the robot. To this end, we will first introduce a quantitative motion feasibility index and then a motion adaptation method based on the index in the following sections.

IV. GENERAL MOTION FEASIBILITY INDEX

In this section, we present a general quantitative index of motion feasibility. The index not only tells whether or not a given motion is feasible for the robot but also quantifies how far the motion is from being infeasible/feasible.

A. Definition

The first six equations in the full-body dynamics equation (1) describe the motion of the floating base and do not involve joint torques, which corresponds to the fact that the total linear and angular momenta are affected only by external forces. Extracting the first six equations of (1) yields

$$\boldsymbol{M}_1 \ddot{\boldsymbol{q}} + \boldsymbol{c}_1 = \boldsymbol{J}_1^T \boldsymbol{w} \tag{7}$$

where $M_1 \in \mathbb{R}^{6 \times N_G}$ and $J_1^T \in \mathbb{R}^{6 \times 6N_C}$ consist of the first six rows of M and J^T , respectively, and c_1 comprises the first six components of c. Substituting (5) into (7) yields

$$M_1\ddot{q} + c_1 = Gf \tag{8}$$

where $\boldsymbol{f} = \begin{bmatrix} \boldsymbol{f}_1^T & \boldsymbol{f}_2^T & \cdots & \boldsymbol{f}_{N_C}^T \end{bmatrix}^T \in \mathbb{R}^{3N_f}$ consists of the contact forces applied to all contact links and is called the total contact force, $\boldsymbol{G} = \begin{bmatrix} \boldsymbol{G}_1 & \boldsymbol{G}_2 & \cdots & \boldsymbol{G}_{N_C} \end{bmatrix} \in \mathbb{R}^{6 \times 3N_f}$ with $\boldsymbol{G}_i = \boldsymbol{J}_{1i}^T \boldsymbol{R}_i \in \mathbb{R}^{6 \times 3N_i}$ maps all contact forces to the wrench around the floating base and is called the total contact mapping, and $N_f = \sum_{i=1}^{N_C} N_i$ is the number of contact forces/points over all contact links.

Given a reference motion for the robot, the left-hand side of (8) can be calculated and it is the required wrench at the floating base for the robot to realize the reference motion. The right-hand side of (8) is the wrench that can be generated on the floating base by contact forces. Matrix G can be calculated based on the state and the position of every contact link specified in the reference motion. Then, whether the reference motion is feasible for the robot is equivalent to whether there are feasible contact forces f, namely contact forces satisfying the friction constraint (4), to generate the required wrench and make (8) hold. To define the motion feasibility index, we look closely at the geometric property of (8). The left side of (8) is a single point w in the 6-D wrench space. The friction constraint (4) defines a convex cone that restricts the contact force at every contact point, as depicted in Fig. 1. Through the linear mapping G, the image of the convex cones from all contact points is a convex cone V with apex at the origin in the 6-D wrench space, which consists of all wrenches that can be generated on the floating base with feasible contact forces. Then, the reference motion is feasible for the robot if and only if the single point w is contained in the convex cone V. If $w \notin V$ or the motion is infeasible, we use the minimum distance d^+ from w to V, defined as below, to measure how far the motion is from being feasible:

$$d^+ \triangleq \min_{\boldsymbol{v} \in V} \|\boldsymbol{w} - \boldsymbol{v}\| \tag{9}$$

where $\|\cdot\|$ denotes the Euclidean norm. If $w \in V$ or the motion is feasible, we use the minimum distance d^- from w to the boundary of V to measure how far the motion is from becoming infeasible:

$$d^{-} \triangleq \min_{\boldsymbol{v} \in \partial V} \|\boldsymbol{w} - \boldsymbol{v}\|$$
(10)

where ∂V denotes the boundary of V. Finally, the motion feasibility index is defined as

$$d \triangleq \begin{cases} d^+ & \boldsymbol{w} \notin V \\ -d^- & \boldsymbol{w} \in V. \end{cases}$$
(11)

Note that d is positive for an infeasible motion and non-positive for a feasible motion.

B. Computation

Now we discuss the algorithms to compute d^+ and d^- . We first assume that the reference motion is infeasible and calculate d^+ . If $d^+ = 0$, which implies that $w \in V$ and the reference motion is feasible, then we continue to calculate d^- . In the following discussion, we denote by V_k a finite set of vectors in V and $CO(V_k)$ the convex cone with apex at the origin formed by vectors in V_k as its edges.

1) Computation of d^+ : The value of d^+ can be calculated by the algorithm [27], which iteratively changes a simplicial cone in V such that its minimum distance from the point wconverges to d^+ , as illustrated in Fig. 2a.

The algorithm [27] starts with any linearly independent set V_k of vectors in V and iterates as follows. Assume that w is not contained in $CO(V_k)$. Let d_k be the minimum distance from w to $CO(V_k)$ and v_k the point on $CO(V_k)$ closest to w, which can be calculated simply by projecting w onto every face of $CO(V_k)$. Let \hat{V}_k be the minimal subset of V_k forming the face of the lowest dimension of $CO(V_k)$ that contains the point v_k . If $v_k \neq w$, then the hyperplane with normal $w - v_k$ passing through v_k bounds $CO(V_k)$ to one side and cuts the convex cone V, which allows us to find a vector on the boundary of V that falls on the other side of the hyperplane. Adding the vector to \hat{V}_k , we obtain V_{k+1} and can prove that the minimum distance d_{k+1} from w to $CO(V_{k+1})$ is strictly smaller than d_k . Therefore, d_k is strictly decreasing



Fig. 2. Computation of the motion feasibility index. (a) Computing d^+ : A simplicial cone $CO(V_k)$ in the convex cone V is changed iteratively such that its minimum distance from the point w converges to the minimum distance d^+ from w to V. (b) Computing d^- : A polyhedral cone $CO(V_k)$ in the convex cone V is expanded iteratively such that the minimum distance from the point w to its boundary converges to the minimum distance d^- from w to the boundary of V.

along with the iteration and guaranteed to converge to d^+ , which is the greatest lower bound on d_k .

If $w \notin V$ or the reference motion is infeasible, then $d^+ > 0$ and the computing of the motion feasibility index d stops; otherwise, $d^+ = 0$ and we continue to compute d^- .

2) Computation of d^- : If $w \in V$ or the reference motion is feasible, then the algorithm [27] yields a finite set V_k of vectors in V such that w is contained in the polyhedral cone $CO(V_k)$. Starting with such a set, which is rewritten as V_0 here, we present an algorithm to compute d^- by iteratively adding vectors to V_k and expanding $CO(V_k)$ such that the minimum distance from w to the boundary of $CO(V_k)$ converges to d^- , as illustrated in Fig. 2b.

Assume that V_0 contains six linearly independent vectors such that the formed polyhedral cone is 6-D in the 6-D wrench space. Let $V_{k,j}$ $(j = 1, 2, ..., N_k)$ be a subset of five linearly independent vectors in V_k that form a facet of $CO(V_k)$. Let $v_{k,j}$ be the orthogonal projection of w on the subspace spanned by $V_{k,j}$ and $d_{k,j}$ the Euclidean distance between w and $v_{k,j}$, which gives the distance from w to the facet formed by $V_{k,j}$. Let $j_k = \arg \min_{j=1,2,...,N_k} d_{k,j}$, $d_k = d_{k,j_k}$ and $v_k = v_{k,j_k}$. Then, it can be proved that d_k , as the minimum distance from w to all the facets of $CO(V_k)$.

The hyperplane with normal $v_k - w$ passing through v_k bounds $CO(V_k)$ to one side. If the hyperplane cuts the convex cone V, then we can find a vector on the boundary of V that is on the other side of the hyperplane. Adding such a vector to V_k yields V_{k+1} , which forms a bigger polyhedral cone $CO(V_{k+1})$ that contains facet j_k of $CO(V_k)$ in its interior. Then, by the iteration, $CO(V_k)$ keeps expanding and d_k is increasing. On the other hand, d^- is the least upper bound on d_k , since $CO(V_k)$ is always contained in V. Therefore, d_k converges to d^- as the algorithm iterates.



Fig. 3. Processing of reference motion. (a) Interpolation of key frames (black dots). To interpolate the motion trajectory between frames 2 and 3 (or 3 and 4 or 4 and 5), frames 1–4 (or 2–5 or 3–6) are used. (b) Time warping of frames 4–6. The motion trajectory is changed since frame 2.

V. TIME WARPING

In this section, we introduce a method for adapting a reference human motion to a humanoid robot based on the proposed motion feasibility index. Unlike most methods that change the pose of the robot in the motion, our method warps the time line of the motion and is called time warping. By doing this, the robot will need to realize the same pose as in the reference motion, which is particularly important for some locomotion tasks that do not allow the robot to deviate from the desired motion, such as following a preplanned footstep sequence or a collision-free trajectory to walk over a rough terrain or through obstacles.

A. Basic Idea

To better understand how time warping works, we first introduce the constitution of a reference motion. A reference motion mainly consists of key motion frames for every DoF of the robot including the floating base and joints. It also contains the time of contact state change for every contact link. The time interval between two frames (typically $\frac{1}{30}$ second) is usually much longer than the control cycle (1 or 2 milliseconds). Then, the trajectory between two frames is determined through interpolation, as depicted in Fig. 3a, which involves not only the two but also several adjacent frames depending on the interpolation method.

Fig. 3b depicts the principle of time warping. Time warping is to alter the times of motion frames, which means that the robot will realize the same pose specified by a motion frame at a different time. Then, the motion trajectory over time, particularly the velocity and the acceleration, will be changed. By doing this, an infeasible reference motion can be turned into a feasible one for the robot.

B. Canonical Time Warping Functions

We first define a canonical time warping function as $t' = f_0(t)$: $t \in [0, 1] \rightarrow t' \in [0, 1]$ with the following properties:

a)
$$f_0(0) = 0;$$

- b) $f_0(1) = 1;$
- c) f_0 is strictly increasing in [0, 1].

The first two properties ensure that the time warping function does not increase or decrease the motion period, while the third property ensures that time warping does not change the order of motion frames over time.

We write a canonical time warping function as a combination of a set of basis functions

$$f_0(t) = \sum_{k=1}^{K} c_k f_k(t)$$
 (12)

where $f_k(t)$'s are user-specified basis functions and c_k 's are unknown coefficients that need to be determined. From (12) with properties a) and b) we obtain

$$\begin{bmatrix} f_1(0) & f_2(0) & \cdots & f_K(0) \\ f_1(1) & f_2(1) & \cdots & f_K(1) \end{bmatrix} \boldsymbol{c} = \begin{bmatrix} 0 \\ 1 \end{bmatrix}$$
(13)

where $\boldsymbol{c} = [c_1 \quad c_2 \quad \cdots \quad c_K]^T$. Then, \boldsymbol{c} can be written as

$$\boldsymbol{c} = \boldsymbol{c}_0 + \boldsymbol{N}\boldsymbol{\lambda} \tag{14}$$

where c_0 is a particular solution and $N\lambda$ is the homogeneous solution to (13).

Property c) is equivalent to the condition $f'_0(t) > 0$ for $\forall t \in [0, 1]$, where $f'_0(t)$ denotes the derivative of $f_0(t)$. We approximate this condition by taking a finite number of sample points t_l (l = 1, 2, ..., L) in [0, 1] and rewrite it as

$$Ac > 0 \tag{15}$$

where

$$\boldsymbol{A} = \begin{bmatrix} f_1'(t_1) & f_2'(t_1) & \cdots & f_K'(t_1) \\ f_1'(t_2) & f_2'(t_2) & \cdots & f_K'(t_2) \\ \vdots & \vdots & \ddots & \vdots \\ f_1'(t_L) & f_2'(t_L) & \cdots & f_K'(t_L) \end{bmatrix}.$$

Substituting (14) into (15) yields

$$AN\lambda > -Ac_0. \tag{16}$$

Equation (16) defines a convex feasible region for λ . By sampling the feasible region and substituting obtained feasible λ 's into (14), we derive valid canonical time warping functions that possess all the three properties for a chosen set of basis functions. Fig. 4 shows the case of valid canonical time warping functions using basis functions t, t^2 , and t^3 .



Fig. 4. Example of canonical time warping function: $f_0(t) = c_1 t + c_2 t^2 + c_3 t^3$. (a) Feasible region (outlined by the red line) and samples (green asterisks) of coefficients such that $f_0(t)$ is strictly increasing in [0, 1]. (b) Plots of corresponding valid canonical time warping functions.

C. Optimization for a Time Warping Function

Assume that a reference motion is infeasible between time t_s and t_e ($t_e > t_s$) and we use a time warping function to modify the segment. Based on a valid canonical time warping function $f_0(t)$, we can write the time warping function f(t) for the segment between t_s and t_e as

$$f(t) = f_0 \left(\frac{t - t_s}{t_e - t_s}\right) (t_e - t_s) + t_s.$$
 (17)

Thanks to the three properties of $f_0(t)$ given in the previous subsection, f(t) possesses the following properties:

- a) $f(t_s) = t_s;$
- b) $f(t_e) = t_e;$
- c) f(t) is strictly increasing in $[t_s, t_e]$.

After choosing the time warping function f(t), we verify and quantify the feasibility of the modified motion between $t_s - \Delta t$ and $t_e + \Delta t$ by the maximum value of the motion feasibility index over the motion segment, where $\Delta t > 0$. It should be noted that, even though the time warping function changes only the times of motion frames between t_s and t_e , the velocity and acceleration of the motion before t_s and after t_e may also be changed because motion frames between



Fig. 5. Values of the motion feasibility index for the original and modified side stepping motion. The original motion becomes infeasible (index being positive) when the right foot of the robot (a) starts to lift off or (b) is about to touch down or the left foot (c) starts to lift off or (d) is about to touch down. By time warping, the modified motion is completely feasible for the robot (index being negative all the time).

 t_s and t_e are also used in the interpolation to determine the motion trajectory before t_s and after t_e , as illustrated in Fig. 3. The time Δt depends on how many motion frames are used in interpolation, which determines how long period of the motion before t_s or after t_e will be affected by changing the times of motion frames between t_s and t_e .

For a chosen set of basis functions, we may have many valid canonical time warping functions, as shown in Fig. 4b, which provide multiple choices of the time warping function for an infeasible motion segment. Among all the time warping functions we seek the one such that the maximum value of the motion feasibility index is minimal. Hopefully, the minimum value is non-positive, which means that the modified motion becomes feasible; otherwise, we may try different basis functions for time warping.

VI. SIMULATION RESULTS

Here we verify the effectiveness of the proposed method through simulation with different motions. The dynamics simulator with rigid-contact model developed by University of Tokyo [25], [24] is used to conduct our experiments. The humanoid robot model used in the simulations has 25 joints (7 in each leg, 4 in each arm, and 3 in the torso) and 31 DoF including the translation and rotation of the floating base. The motion tracking controller proposed in [28] is used for the robot to reproduce a reference motion.

A. Side Stepping

We first use a side stepping motion to demonstrate our method. Fig. 5 plots the value of the motion feasibility index for the motion. It can be seen that the index is positive at some moments, which implies that the motion is not entirely feasible for the robot. We take the time warping function to be a cubic function for every infeasible motion segment. Then, the index for the modified motion becomes all negative (Fig. 5), which implies that the motion becomes feasible after time warping. Fig. 6a shows the snapshots comparing the original and modified motions. It can be observed that time warping accelerates the robot's body motion towards one supporting foot side while the other foot is about to lift off.



Fig. 7. Values of the motion feasibility index for the original and modified walking upstairs motion.

This ensures that the weight of the robot can be supported by only one foot after the other foot lifts off and the robot will not lose balance. Similarly, while the liftoff foot is about to touch down, the robot's body motion is slowed down, which wins the time for the liftoff foot to touch down. Fig. 6b shows the snapshots of the simulated motion when the robot tries to reproduce the modified motion. It can be seen that there is no significant difference between the two motions and the robot is able to reproduce the stepping motion well. The original, modified, and simulated motions are also shown in the accompanying video.

B. Walking Upstairs

Thanks to the general motion feasibility index, the proposed motion adaptation method can be applied to motions on any terrain. In this example, we let the robot mimic a human walking upstairs, where each stair is about 0.083 m high. Fig. 7 shows the values of the motion feasibility index for the original and modified motions. Cubic functions are selected as the time warping functions, which successfully turn all the infeasible motion segments into feasible ones. The comparison between the original and modified motions and between the modified and simulated motions is exhibited in Fig. 8 and the accompanying video.

C. Walking Downstairs

Similarly to the previous example, the robot is required to walk downstairs in this example. The value of the motion feasibility index is plotted in Fig. 9. The motions are shown in Fig. 10 and the video. Though the modified motion is still infeasible at some moments, its index value is just slightly above zero and the motion is very close to a feasible motion. This small extent of infeasibility for such a short period can be well handled by the motion tracking controller and the robot can get back on track before going too far. That is why the simulated motion has no big deviation from the modified motion, as shown in Fig. 10b and the accompanying video.

VII. CONCLUSION AND FUTURE WORK

This paper presents a method based on time warping for adapting human motions to humanoid robots by changing the time line of the motion. An advantage of this method is that it only changes the velocity and acceleration profiles of





(b)

Fig. 6. Snapshots of side stepping. (a) Comparison of modified (solid) and original (transparent) motions. (b) Comparison of simulated (solid) and modified (transparent) motions.



Fig. 8. Snapshots of walking upstairs. (a) Comparison of modified (solid) and original (transparent) motions. (b) Comparison of simulated (solid) and modified (transparent) motions.

the motion and allows the robot to realize the same poses as in the reference motion. A general motion feasibility index is proposed to identify infeasible motion segments for the robot in the reference motion. Then, each infeasible motion segment is modified through time warping. The proposed method has been tested on different human motions and is able to find feasible motions in most cases or at least bring an infeasible motion close to a feasible one, which makes it easier and safer for the robot to reproduce those motions.

This work can be extended in many directions. First, the choice of a time warping function can be arbitrary. However, it can be seen from Fig. 4b that a time warping function can either first speed up and then slow down the motion or do the reverse. It might be possible to identify whether a motion needs to be sped up or slowed down first to make it feasible, which will reduce the search scope of time warping functions

and facilitate the use of this method. Second, the proposed motion feasibility index is general and applicable to motions happening on any terrains or the case that a humanoid robot needs to contact the environment with links other than feet. Hence, the method will be tested on more challenging human motions. Third, we currently modify a motion in the time domain. We can modify a motion in the joint or operation space as well based on the general motion feasibility index, which will also be investigated in the future.

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Fig. 10. Snapshots of walking downstairs. (a) Comparison of modified (solid) and original (transparent) motions. (b) Comparison of simulated (solid) and modified (transparent) motions.



Fig. 9. Values of the motion feasibility index for the original and modified walking downstairs motion.

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